Large amplitude collective motion in ${}^{44}S^{\dagger}$

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It is well known that neutron-rich $N \simeq 28$ nuclei exhibit strong quadrupole collectivity.^{1,2)} Using antisymmetrized molecular dynamics (AMD), we have discovered many interesting features such as triaxial deformation and shape coexistence in ⁴²Si and neighboring nuclei.^{3,4)} Herein, we report the large-amplitude collective motion (LACM) in ⁴⁴S.

Figure 1 shows the comparison between the energy curves and collective amplitudes of ⁴⁰Mg and ⁴⁴S. ⁴⁰Mg possesses the prolately-deformed energy minimum and the collective amplitude of the ground state is localized around it, whereas the 0_2^+ state is localized in the oblately-deformed region. Thus, ⁴⁰Mg depicts the coexistence of the prolate and oblate rigid rotors. In contrast, ⁴⁴S exhibits a significantly different structure: The energy curve is extremely flat as a function of γ and the collective amplitudes of the ground, and the 0_2^+ states demonstrate broad and non-localized distributions, which imply that ⁴⁴S possesses no rigid shape due to the LACM.



Fig. 1. Energy curves and collective amplitudes of the 0_1^+ and 0_2^+ states as functions of the quadrupole deformation parameter γ . The values of quadrupole parameter β are set to 0.35 and 0.30 for ⁴⁰Mg and ⁴⁴S, respectively.

A general question is as follows: Based on which type of physical quantity, can we distinguish rigid-rotor and LACM? The monopole transition is the solution to this question. The monopole transition strength (Table 1) is strongly hindered in ${}^{40}Mg$, whereas it is

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Table 1. Electric (E0) and isoscalar (IS0) monopole transition strengths in Weisskopf unit (Wu).

	^{40}Mg	^{44}S (calc.)	$^{44}S (expt.)^{5)}$
$B(E0;0_1^+ \to 0_2^+)$	0.0	0.04	0.022(2)
$B(IS0;0_1^+ \to 0_2^+)$	0.0	0.38	

non-negligible in ⁴⁴S.⁵⁾ This feature can be explained using a two-configuration mixing model.⁶⁾ ⁴⁰Mg possesses prolate ground state and oblate 0^+_2 state; hence, the monopole matrix element is given as $\langle obl. | \mathcal{M} | pro. \rangle$, where $| pro. \rangle$ and $| obl. \rangle$ denote the prolate and oblate configurations, respectively, and \mathcal{M} denotes the transition operator (1p1h operator). This matrix element vanishes because single-particle configurations of $| pro. \rangle$ and $| obl. \rangle$ differ by 2p2h. This is the reason why the transition is strongly hindered in ⁴⁰Mg.

Owing to LACM, we approximate ${}^{44}S$ as a mixture of prolate and oblate shapes with equal amplitudes,

$$0_1^+\rangle = (|\text{pro.}\rangle + |\text{obl.}\rangle)/\sqrt{2},\tag{1}$$

$$0_2^+\rangle = (|\text{pro.}\rangle - |\text{obl.}\rangle)/\sqrt{2}.$$
(2)

In this case, the transition matrix read

$$\langle 0_2^+ | \mathcal{M} | 0_1^+ \rangle = \frac{1}{2} \{ \langle \text{pro.} | \mathcal{M} | \text{pro.} \rangle - \langle \text{obl.} | \mathcal{M} | \text{obl.} \rangle \}$$
(3)

Thus, the transition matrix is proportional to the difference in the squared-radii of the prolate and oblate shapes. Consequently, ⁴⁴S possesses non-negligible monopole transition strength. Using the single AMD wave functions with prolate and oblate deformation and Eq. (3), we obtain B(E0) = 0.05 Wu and B(IS0)= 0.4 Wu, which are close to the results of the full model space calculation listed in Table 1.

Thus, there is an interesting relationship between the monopole transition and LACM. In 40 Mg, the prolate and oblate rotors coexist, and the monopole transition is hindered as they do not mix with each other. In 44 S, there is a considerable mixture of prolate and oblate shapes due to LACM. This leads to the nonnegligible monopole transition, which is roughly proportional to the difference in the squared-radii of the two shapes.

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