# Large amplitude collective motion in ${ }^{44} \mathrm{~S}^{\dagger}$ 

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It is well known that neutron-rich $N \simeq 28$ nuclei exhibit strong quadrupole collectivity. ${ }^{1,2)}$ Using antisymmetrized molecular dynamics (AMD), we have discovered many interesting features such as triaxial deformation and shape coexistence in ${ }^{42} \mathrm{Si}$ and neighboring nuclei. ${ }^{3,4)}$ Herein, we report the large-amplitude collective motion (LACM) in ${ }^{44}$ S.

Figure 1 shows the comparison between the energy curves and collective amplitudes of ${ }^{40} \mathrm{Mg}$ and ${ }^{44} \mathrm{~S}$. ${ }^{40} \mathrm{Mg}$ possesses the prolately-deformed energy minimum and the collective amplitude of the ground state is localized around it, whereas the $0_{2}^{+}$state is localized in the oblately-deformed region. Thus, ${ }^{40} \mathrm{Mg}$ depicts the coexistence of the prolate and oblate rigid rotors. In contrast, ${ }^{44} \mathrm{~S}$ exhibits a significantly different structure: The energy curve is extremely flat as a function of $\gamma$ and the collective amplitudes of the ground, and the $0_{2}^{+}$states demonstrate broad and non-localized distributions, which imply that ${ }^{44} \mathrm{~S}$ possesses no rigid shape due to the LACM.


Fig. 1. Energy curves and collective amplitudes of the $0_{1}^{+}$ and $0_{2}^{+}$states as functions of the quadrupole deformation parameter $\gamma$. The values of quadrupole parameter $\beta$ are set to 0.35 and 0.30 for ${ }^{40} \mathrm{Mg}$ and ${ }^{44} \mathrm{~S}$, respectively.

A general question is as follows: Based on which type of physical quantity, can we distinguish rigid-rotor and LACM? The monopole transition is the solution to this question. The monopole transition strength (Table 1) is strongly hindered in ${ }^{40} \mathrm{Mg}$, whereas it is

[^0]Table 1. Electric ( $E 0$ ) and isoscalar ( $I S 0$ ) monopole transition strengths in Weisskopf unit (Wu).

|  | ${ }^{40} \mathrm{Mg}$ | ${ }^{44} \mathrm{~S}$ (calc.) | ${ }^{44} \mathrm{~S}(\operatorname{expt} .)^{5)}$ |
| :---: | :---: | :---: | :---: |
| $B\left(E 0 ; 0_{1}^{+} \rightarrow 0_{2}^{+}\right)$ | 0.0 | 0.04 | $0.022(2)$ |
| $B\left(I S 0 ; 0_{1}^{+} \rightarrow 0_{2}^{+}\right)$ | 0.0 | 0.38 |  |

non-negligible in ${ }^{44}$ S. ${ }^{5)}$ This feature can be explained using a two-configuration mixing model. ${ }^{6)}{ }^{40} \mathrm{Mg}$ possesses prolate ground state and oblate $0_{2}^{+}$state; hence, the monopole matrix element is given as $\langle$ obl. $| \mathcal{M} \mid$ pro. $\rangle$, where |pro.〉 and |obl.〉 denote the prolate and oblate configurations, respectively, and $\mathcal{M}$ denotes the transition operator ( 1 p 1 h operator). This matrix element vanishes because single-particle configurations of |pro.) and |obl.) differ by 2 p 2 h . This is the reason why the transition is strongly hindered in ${ }^{40} \mathrm{Mg}$.

Owing to LACM, we approximate ${ }^{44} \mathrm{~S}$ as a mixture of prolate and oblate shapes with equal amplitudes,

$$
\begin{align*}
\left|0_{1}^{+}\right\rangle & =(\mid \text {pro. }\rangle+\mid \text { obl. }\rangle) / \sqrt{2}  \tag{1}\\
\left|0_{2}^{+}\right\rangle & =(\mid \text {pro. }\rangle-\mid \text { obl. }\rangle) / \sqrt{2} . \tag{2}
\end{align*}
$$

In this case, the transition matrix read

$$
\begin{equation*}
\left.\left.\left.\left\langle 0_{2}^{+}\right| \mathcal{M}\left|0_{1}^{+}\right\rangle=\frac{1}{2}\{\langle\text { pro. }| \mathcal{M} \mid \text { pro. }\rangle-\langle\text { obl. }| \mathcal{M} \right\rvert\, \text { obl. }\right\rangle\right\} \tag{3}
\end{equation*}
$$

Thus, the transition matrix is proportional to the difference in the squared-radii of the prolate and oblate shapes. Consequently, ${ }^{44} \mathrm{~S}$ possesses non-negligible monopole transition strength. Using the single AMD wave functions with prolate and oblate deformation and Eq. (3), we obtain $B(E 0)=0.05 \mathrm{Wu}$ and $B(I S 0)$ $=0.4 \mathrm{Wu}$, which are close to the results of the full model space calculation listed in Table 1.

Thus, there is an interesting relationship between the monopole transition and LACM. In ${ }^{40} \mathrm{Mg}$, the prolate and oblate rotors coexist, and the monopole transition is hindered as they do not mix with each other. In ${ }^{44} \mathrm{~S}$, there is a considerable mixture of prolate and oblate shapes due to LACM. This leads to the nonnegligible monopole transition, which is roughly proportional to the difference in the squared-radii of the two shapes.

## References

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