## Momentum-space structure of dineutron in <sup>11</sup>Li<sup>†</sup>

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A recent knockout-reaction experiment for the Borromean nucleus <sup>11</sup>Li measured the mean correlation angle between the momenta of emitted neutrons  $n_1$  and  $n_2$  in the reaction channel <sup>11</sup>Li $(p, pn_1)^{10}$ Li<sup>\*</sup>  $\rightarrow$  <sup>9</sup>Li +  $n_2$ .<sup>1)</sup> The dependence on the missing momentum k of  $n_1$  is considered to reflect the spatial structure of dineutron.

Here, the reflection of the spatial structure of dineutron to the mean opening angle between the momenta  $\mathbf{k}_1$  and  $\mathbf{k}_2$  of the valence neutrons at the ground state of <sup>11</sup>Li is discussed. Further, the similarities with the mean correlation angle are highlighted.

A three-body model calculation is performed in the momentum space using a finite-range n-n interaction, which reproduces the two-neutron (2n) separation energy and the matter radius of <sup>11</sup>Li. Further, the 2n density,  $\rho_2(k_1, k_2, \theta_k)$ , is calculated using  $k_1 = |\mathbf{k}_1|$ ,  $k_2 = |\mathbf{k}_2|$ , and the opening angle between  $\mathbf{k}_1$  and  $\mathbf{k}_2$ ,  $\theta_k$ . Figure 1(a) shows  $\rho_2(k_1, k_2, \theta_k)$  as a function of both  $k_1 = k_2 = k_n$  and  $\theta_k$ . Figure 1(b) shows the 2n density in real space via the Fourier transformation,  $\rho_2(r_1, r_2, \theta_r)$ , using the radial coordinates,  $r_1 = r_2 = r$ , and opening angle,  $\theta_r$ .



Fig. 1. (a) 2n density for <sup>11</sup>Li as functions of  $k_1 = k_2 = k_n$ and the opening angle  $\theta_k$ . It is weighted with a factor of  $8\pi^2 k_n^4 \sin \theta_k$ . (b) Same as (a) but 2n density in real space as functions of  $r_1 = r_2 = r$  and the opening angle  $\theta_r$ . It is weighted with a factor of  $8\pi^2 r^4 \sin \theta_r$ .

The dineutron configuration is obtained at the lowmomentum of  $(k_n, \theta_k) = (0.18 \text{ fm}^{-1}, 128^\circ)$ . It is accompanied by the broad angular distribution, and the long  $k_n$ -tail indicates the strong dineutron correlation (the high n-n relative momentum).

The mean opening angle  $\langle \theta_k \rangle$  is defined as a function

of  $k_1 = k_n$  as follows

$$\cos \left\langle \theta_k \right\rangle \equiv \left[ \int_0^{k_{\text{cut}}} k_2^2 dk_2 \int_0^{\pi} 2\pi \sin \theta_k d\theta_k \right. \\ \left. \times \left. \rho_2(k_n, k_2, \theta_k) \cos \theta_k \right] / \rho_k(k_n), \tag{1}$$

where  $\rho_k(k_n)$  is the one-neutron density distribution. Figure 2(a) shows  $\langle \theta_k \rangle$  using the cutoff momenta of  $k_{\text{cut}} = \infty$  (no cutoff) and  $k_{\text{cut}} = k_{\text{surf}} = 0.62 \text{ fm}^{-1}$ .



Fig. 2. (a) Mean opening angle  $\langle \theta_k \rangle$  as a function of  $k_1 = k_n$  for <sup>11</sup>Li. "Surface" indicates the cutoff of  $k_{\text{cut}} = k_{\text{surf}}$ . (b) Same as (a) but for <sup>6</sup>He, <sup>22</sup>C, and <sup>19</sup>B.

 $\langle \theta_k \rangle$  (no cutoff) exhibits a peak at  $k_n = 0.27 \text{ fm}^{-1}$ ; however, it gradually increases above  $k_n \approx 0.5 \text{ fm}^{-1}$ .

 $k_{\rm surf}$  characterizes the low-momentum halo region by  $k_1, k_2 < k_{\rm surf}$ .  $\langle \theta_k \rangle$  using  $k_{\rm cut} = k_{\rm surf}$  exhibits a peak at  $k_n = 0.31 \text{ fm}^{-1}$  and a plateau of  $\langle \theta_k \rangle \approx 82^{\circ}$  above  $k_n \approx 1.0 \text{ fm}^{-1}$ . These features are consistent with the observed k dependence of the mean correlation angle (the peak at  $k \approx 0.3 \text{ fm}^{-1}$  and the plateau of approximately  $87^{\circ}$  above  $k \approx 0.9 \text{ fm}^{-1}$ ),<sup>1)</sup> which is considered to reflect the 2n correlations in the surface region.<sup>2)</sup>

In conclusion, the manner in which the mean opening angle reflects the 2n density in <sup>11</sup>Li was discussed. For  $\langle \theta_k \rangle$ , the importance of the surface effect and the similarities with the mean correlation angle in the knockout reaction were highlighted. The same conclusion was obtained for <sup>6</sup>He, <sup>22</sup>C, and <sup>19</sup>B (see Fig. 2(b)), wherein the measurement of the momentum dependence of the angular correlations between the halo neutrons can provide useful information on dineutron correlations at low density.

## References

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- 2) J. Casal et al., Phys. Rev. C 104, 024618 (2021).

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